

# Word Problems 12: Mixed-Rate Problems #9

P. Reany

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## Abstract

In this algebra word problem note, we use the Scheme to solve our ninth attempt at what I refer to as a ‘mixed-rate problem’. In this type of problem, two or more ‘machines’ work together at generally different rates to produce subtotals that add to a total. Quantitative information can be given in the problem in various forms: percentages, fractional amounts, or by ratios. We have to know how to deal with each of them.

## 1 Introduction

The problems here are fairly routine.

## 2 Word Problem #12.1

$A$  and  $B$  together can do a job in 8 days.  $A$  and  $C$  together can do the job in 9 days. And  $B$  and  $C$  together can do the job in 10 days. What is  $B$ ’s individual rate?

## 3 Solution 12.1.1: Conceptualizing the Problem

When two machines,  $A$  and  $B$ , say, work together over a common time they have a combined effective rate of  $\frac{1}{T}$ , which we get from the equation

$$(R_A + R_B)T = 1[\text{job}], \quad (1)$$

from which we get

$$R_{A+B}^{\text{effective}} = R_A + R_B = \frac{1}{T}. \quad (2)$$

Now, on to the rate we need. So, from the given information, we get

$$R_A + R_B = 1/8, \tag{3a}$$

$$R_A + R_C = 1/9, \tag{3b}$$

$$R_B + R_C = 1/10. \tag{3c}$$

According to wolframalpha.com,  $R_B = \frac{41}{720}$ .

## 4 Word Problem #12.2

A woman sold 100 oranges for \$12.10 total. She sold the first kind at the rate of 3 for 35¢ and the second kind at the rate of 7 for 85¢. How many were sold at the first rate?

### 5 Solution 12.2.1: Conceptualizing the problem

Let's begin with a figure this time.

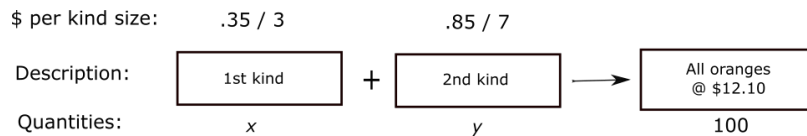


Figure 1. We've converted the cents sign to dollars. Otherwise, the problem is quite familiar to us by now.

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Next, we write the familiar 'total as sum of its parts' equation:

$$(\text{Total sales from oranges}) = (\text{sales from 1st kind}) + (\text{sales from 2nd kind}). \tag{4}$$

Then, suppressing units, we get

$$12.10 = \frac{.35}{3} x + \frac{.85}{7} y. \tag{5a}$$

We also have the conservation equation on the total number of oranges:

$$100 = x + y. \tag{5b}$$

Combining (5a) and (5b), we get the solution for the first kind sold as  $x = 9$  oranges.

## 6 Word Problem #12.3

Question 224473:<sup>1</sup> Three skilled laborers  $a$ ,  $b$ , and  $c$  can do a job in 20 days. Just  $a$  and  $b$  can do the job in 30 days. Just  $b$  and  $c$  can do the job in 40 days. What are their individual rates in units job/days?

## 7 Solution 12.3.1: Conceptualizing the Problem

This problem is similar to Problem 12.1 above. We won't need a figure this time, either. Let  $x = R_a$ ,  $y = R_b$ ,  $z = R_c$ . Then we get the three equations:

$$20(x + y + z) = 1, \quad (6a)$$

$$30(x + y) = 1, \quad (6b)$$

$$40(y + z) = 1. \quad (6c)$$

Solving these together [using wolframalpha.com], we get

$$R_a = 1/40 \text{ [job/day]},$$

$$R_b = 1/120 \text{ [job/day]},$$

$$R_c = 1/60 \text{ [job/day]}.$$

## 8 Word Problem #12.4

A shop keeper wants to make 4 pounds of a tea blended from two ingredients: black tea, costing \$2.20 per pound, and orange pekote tea, costing \$3.00 per pound. If the value of the blended tea is to be \$2.50 per pound, how much of the ingredients are to be use to maintain the value of the ingredients in the blend?

## 9 Solution 12.4.1: Conceptualizing the Problem

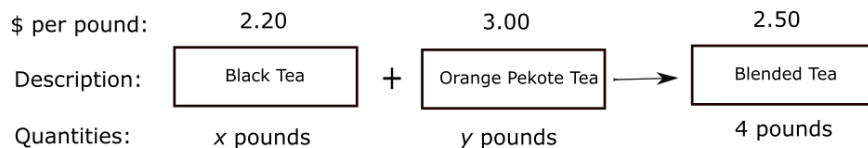


Figure 2. We'll be writing conservation equations on both poundage and cost, or value, on the teas, before and after blending.

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<sup>1</sup>Found at <https://www.algebra.com/algebra>.

## 10 Solution 12.4.2: Solving the Problem

Now we extract the equations we need.

$$\begin{array}{ll} \text{Conservation of poundage:} & x + y = 4, \\ \text{Conservation of cost (value):} & 2.20x + 3.00y = 2.50(4). \end{array}$$

The solution for this couple of equations is:  $x = 2.5$ , and  $y = 1.5$ , both in pounds, of course.

## 11 Conclusion

Wolframalpha.com has become my 'graphing calculator.'